# Effect of rubber particle size on the impact tensile fracture behavior of MBS resin with a bimodal particle size distribution

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Abstract We performed impact tensile fracture experiments on methylmethacrylate–butadiene–styrene (MBS) resin with small and large particles in a bimodal size distribution, and examined the effects of particle size on fracture behavior by fixing the total rubber content (28 wt%) and the small particle size (about 140 nm), and varying the size of large particles (about 490 nm or 670 nm). Dynamic load  $P'$  and displacement  $\delta'$  of singleedge-cracked specimens were measured using a Piezo sensor and a high-speed extensometer, respectively. A  $P'$ – $\delta'$  diagram was used to determine external work  $U_{\text{ex}}$ applied to the specimen, elastic energy  $E<sub>e</sub>$  stored in the specimen, and fracture energy  $E_f$  for creating a new fracture surface  $A_s$ . Energy release rate was then estimated using  $G_f = E_f/A_s$ . Values of  $G_f$  were correlated with fracture loads and mean crack velocity  $v_m$  determined from load and time relationships. We then examined the effect of particle size on  $G_f$  and  $v_m$ , and results indicated that particle size plays an important role in changing the values of  $G_f$  and  $v_m$ .

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## Introduction

Particle dispersion methods have been widely applied on many types of materials to improve their mechanical reliability. For example, brittle polymers exhibit increased impact resistance when rubber particles are dispersed in resin matrix. This method has been used on materials including high impact strength polystyrene (HIPS) and acrylonitrile–butadiene–styrene (ABS) resin, and studies have verified its validity and applicability. The mechanisms of fracture behavior in these materials have also been investigated from micro- and macroscopic perspectives. Rubber particles reportedly play an important role in enhancing impact resistance by generating crazes, shear bands, and cavitations around particles near a crack front in the material  $[1-3]$ . The same method has been employed to increase impact resistance in a transparent polymer, methylmethacrylate–butadiene–styrene (MBS) resin [\[4–7](#page-6-0)]. However, rubber particles in the resin deteriorate important material properties such as transparency and rigidity or modulus. Therefore, it is critically important to design and optimize the size of rubber particles, total rubber content, and the refractive index of the particles. Recent studies have investigated the effect of a bimodal distribution of rubber particle sizes and its validity and applicability [\[4–7](#page-6-0)]. Takahashi et al. [\[5](#page-6-0), [6](#page-6-0)] studied this problem using two kinds of MBS resins and reported that the bimodal distribution improves not only the falling weight impact strength but also the transparency of the resin. They also suggested that the bimodal particle size plays an important role in generating microscopic shear bands and cavitations around and between the small and large particles near a crack front under the impact loading [\[5](#page-6-0), [6\]](#page-6-0).

We examined the fracture behavior of MBS resin with a bimodal rubber particle size distribution. To examine the effects of particle size, the total rubber content (28 wt%) and the size of small particles (about 140 nm) were unchanged and the size of large particles were either about 490 nm or 670 nm. Single-edge-cracked tensile specimens were fractured under impact tensile loading, and impact load and specimen displacement were measured using a Piezo sensor [[8\]](#page-6-0) and high-speed extensometer [[9\]](#page-6-0), respectively, to evaluate external work  $U_{\text{ex}}$  applied to the specimen. Elastic energy  $E_e$  and nonelastic energy  $E_n$  were estimated from the oscillation of the split specimen just after fracture. Fracture energy  $E_f$  was then determined and correlated with fracture load  $P_c$ . For fracture surface  $A_s$ , the energy release rate was evaluated using  $G_f = E_f/A_s$ . Mean crack velocity  $v_m$  was also estimated as a function of  $P_c$ . This paper presents the results and discusses the effects of large particle sizes.

#### Specimen material

Experiments were conducted on MBS resin with a bimodal rubber particle size distribution provided by Denki Kagaku Kogyo. Figure 1 shows the resin microstructure, and Table 1 lists the average rubber particle diameters and weight fractions. The resin matrix was the copolymer of methylmethacrylate–styrene, and rubber particles were prepared by a graft polymerization of styrene monomer and (meth)acrylate monomer on styrene–butadiene rubber. Large rubber particles were prepared by carrying out bulk polymerization of the monomers in dissolved styrene– butadiene rubber (rubber content 10 wt%) by stirring, while small rubber particles were prepared by performing emulsion polymerization of the monomers in a latex of styrene–butadiene rubber (rubber content 70 wt%) [[5\]](#page-6-0).

In this experiment, total rubber content (28 wt%) and small particle size (about 140 nm) were unchanged, but the size of large particles was either about 490 nm or 670 nm.



Table 1 Weight fractions of rubber particles in MBS resin

Diameter (nm)	Large particle		Small particle
	490	670	140
Sample-1 $(wt\%)$	70		30
Sample-2 ( $wt\%$ )		70	30

The composition of rubber/poly(meth)acrylate/polystyrene was 28/31/41, the average molecular weight was 150,000, the melt flow index under 200  $^{\circ}$ C and 5 kg was 1.5 g per 10 min, and the glass transition temperature was about 90 °C. The dumbbell-type specimens were injection-molded from pellets after melting extrusion. When large particle size increased, transparency of the specimen deteriorated slightly because the larger particles affected surface flatness. However, no changes were observed in their static material properties. The yield stress, fracture stress and strain under tensile loading were 34 MPa, 25 MPa and 40%, respectively. This suggests that total rubber content is an influential parameter in determining the static properties. No big difference was also observed on the dispersion of the particles between the pellets and specimens since the particles with cross-linked structure were not deformed significantly during the injectionmolding. Figure  $2(a)$  $2(a)$  illustrates the specimen geometry. To change the fracture initiation load of specimens or external work applied to the specimen, sharp pre-cracks with lengths varying from about 1–4.5 mm were generated by forcing a razor blade into a pre-machined saw-cut on the specimen's edge. By varying this distance, values of the mean crack velocity in the specimens were also varied.

## Experimental methods

An impact tensile load was introduced using a special loading device that utilizes the free-fall of a weight [[8\]](#page-6-0). As illustrated in Fig. [2](#page-2-0)(b), this device consists of an electromagnet that holds the weight at an arbitrary height, a metal frame for converting the impulse force into tension, loading axes for mounting the specimen, and a Piezo sensor for measuring the impact load. The specimen was clamped rigidly at its lower and upper parts to satisfy the requirements for specimen symmetry. A 3–mm-thick rubber sheet was mounted on the upper end of the frame to attenuate high-frequency vibrations caused by the impact.

All specimens were loaded by dropping a 10-kg weight from a height of 300 mm, so that the impact velocity of the weight was about 2.4 m/s. The sensor had a frequency response of 45 kHz, so it permitted dynamic measurements [\[8](#page-6-0)]. Load P applied to each specimen was partitioned into Fig. 1 Microstructure of MBS resin (Sample-1) an initial static load  $P_0$  due to the metal frame's dead <span id="page-2-0"></span>Fig. 2 Specimen geometry and experimental setup for loading and displacement measurement (a) Specimen geometry, (b) Loading method,

(c) Displacement measurement



(a) Specimen geometry

(c) Displacement measurement

weight, and a dynamic load  $P'$  due to the impact (see Fig. 2(b)). Tests were conducted at room temperature, and deformation of the loading axis was disregarded because it was much stiffer than the specimen. Displacement  $\delta$  at the specimen's centerline was also evaluated and partitioned into an initial static value  $\delta_0$  and a dynamic value  $\delta'$ .

Figure 2(c) illustrates the configuration for displacement measurement using an optical fiber and a position-sensing detector (PSD) (SiTek Electro Optics). In this experiment, the fiber was attached to the upper region at a point 2 mm from the pre-crack to avoid damage caused by dynamic crack propagation. However, this influence on dynamic displacement  $\delta'$  was disregarded because measurements were likely only a few percent smaller than they would have been at the specimen's centerline. A laser diode was used as a light source, and an amplifier and digital wave memory were used to record output signals from the PDS. The PSD is an optoelectronic device that converts an incident light spot into continuous position data using the lateral photo effect, and it has a frequency response of 100 kHz, so it permitted both static and dynamic displacement measurements [\[9](#page-6-0)].

#### Definition of fracture energy

Figure 3 plots load P versus displacement  $\delta$  for the frame's dead weight (see Fig. 2(b)). In this figure,  $P_0$  and  $\delta_0$  indicate initial static values due to the dead weight, and  $P_c$  and  $\delta_c$  denote critical dynamic values at the onset of fracture. Although  $P-\delta$  relationships generally differ between static and dynamic loads, this analysis assumed they were identical for simplicity. External work  $U_{\text{ex}}$  applied to half the specimen is then given as

$$
U_{\rm ex} = \frac{P_{\rm c}\delta_{\rm c}}{2} = \frac{\delta_{\rm c}'(P_{\rm o} + P_{\rm c}')^2}{2P_{\rm c}'},\tag{1}
$$



Fig. 3 Load P versus displacement  $\delta$  diagram for a specimen with initial load  $P_0$ 

where  $P_c = P_o + P_c'$  and  $\delta_c = \delta_c' P_c/P_c'$ . Equation (1) is valid when  $P_0$  and  $\delta_0$  are much smaller than  $P_c$  and  $\delta_c$ , and nonlinearity due to the material's viscoelastic and plastic deformation during impact is not significant.

This analysis also assumed that  $U_{\text{ex}}$  can be partitioned into three regions, as shown in Fig. 3 [[10,](#page-6-0) [11](#page-6-0)]:

$$
U_{\rm ex} = E_{\rm f} + E_{\rm e} + E_{\rm n}, \qquad (2)
$$

where  $E_f$  is the fracture energy created for half the new surfaces  $2A_s$  which includes the energy loss due to the generation of microscopic shear bands and cavitations near the surfaces,  $E_e$  is the specimen's elastic energy, and  $E_n$  is the nonelastic energy of the specimen material due to the viscoelastic and plastic deformation [\[10](#page-6-0), [11\]](#page-6-0).

 $E_e$  and  $E_n$  were determined under the following assumptions. First,  $E_e$  was converted into the kinetic energy of the split specimen after fracture. Then, the material's viscosity could be neglected during dynamic crack propagation [\[12](#page-6-0)], so the change from  $P_c$  to  $\delta_e$  or  $\delta_n$  was elastic (see Fig. 3). Finally, the following relationships held:

<span id="page-3-0"></span>

Fig. 4 Dynamic load  $P'$  as a function of time t (sampling time  $\Delta t = 1$  µs)

$$
\frac{E_{\rm e}}{U_{\rm ex}} = \frac{(\delta_{\rm e} - \delta_{\rm n})}{\delta_{\rm c}}, \frac{E_{\rm n}}{U_{\rm ex}} = \frac{\delta_{\rm n}}{\delta_{\rm c}}.
$$
\n(3)

#### Results and discussion

Dynamic load  $P'$  and displacement  $\delta'$ 

The Piezo sensor was used to measure the dynamic load  $P'$ applied to the specimen (see Fig.  $2(b)$  $2(b)$ ). Figure 4 plots the value of  $P'$  as a function of time t, showing experimental results of two samples with almost identical initial crack lengths. P' increased with t, and then fell abruptly from  $P_c'$ as the crack started to propagate. Note that sample-2 yielded much greater  $P_c'$  values than sample-1.

In this experiment, fracture load  $P_c'$  was determined from six specimens of each sample. The results obtained from single tests were plotted in Fig. 5 as a function of the initial crack length  $a_0$ .  $P_c'$  decreased with  $a_0$ , but sample-2 yielded greater  $P_c'$  values than sample-1 for a given  $a_0$ , suggesting that fracture behavior could be changed by increasing the size of large particles from about 490 to about 670 nm even when the rubber content is identical.



Fig. 6 Dynamic displacement  $\delta'$  as a function of time t (sampling time  $\Delta t = 1 \text{ }\mu\text{s}$ 

Figure 6 illustrates dynamic displacement  $\delta'$  measured using the optical fiber and PSD (see Fig.  $2(c)$  $2(c)$ ). As shown in the figure,  $\delta'$  increased with time t, and then fell abruptly as the fracture initiated at the critical value  $\delta_{c}$ . After fracture,  $\delta'$  exhibited damping oscillation. Note that sample-2 yielded greater  $\delta_c'$  values than sample-1, similar to findings for fracture load  $P_c'$  (see Fig. 4).

Figure 7 plots the variation in critical displacement  $\delta_c'$ versus load  $P_c'$ .  $\delta_c'$  increased with  $P_c'$ , suggesting they had a linear relationship, and sample-2 yielded greater  $\delta_c'$ values than sample-1 for a given  $P_c'$ . This implies that the large particles can increase specimen elongation to fracture under impact different from the static loading conditions.

## External work  $U_{\text{ex}}$

Figure [8](#page-4-0) illustrates the relationship between dynamic load  $P'$  and displacement  $\delta'$  for sample-1 determined from Figs. 4 and 6. Although a slight change appeared in the  $P'$ – $\delta'$  diagram, we assumed a linear relationship between  $P'$  and  $\delta'$ , as shown in Fig. [3.](#page-2-0) Since the conditions were the same for sample-2, external work  $U_{\text{ex}}$  was evaluated using Eq. (1). In Fig. [8](#page-4-0), the dynamic external work  $U_{\rm ex}$ ' is partitioned into two regions of the elastic energy  $E_e'$  and



Fig. 5 Fracture load  $P_c'$  versus initial crack length  $a_0$ 



Fig. 7 Critical displacement  $\delta_c'$  as a function of fracture load  $P_c'$ 

<span id="page-4-0"></span>

Fig. 8 The relationship between dynamic load  $P'$  and displacement  $\delta'$ 

fracture energy  $E_f'$ , and the nonelastic energy  $E_n'$  is disregarded. The reason for this will be discussed later.

Figure 9 plots the variations in external work  $U_{\rm ex}$  versus load  $P_c$  (= $P_o + P_c'$ ). As the figure illustrates,  $U_{ex}$  increased with  $P_c$ , indicating that sample-2 had a greater  $U_{ex}$  value than sample-1 for a given  $P_c$ . This suggests that changing the size of large particles can increase fracture energy.

#### Elastic energy  $E_e$

The elastic displacement  $\delta_e$  must be determined to evaluate a specimen's elastic energy  $E_e$  (see Fig. [3](#page-2-0)). This was achieved by measuring displacement  $\delta'$  beside the crack position before and after fracture (see Fig.  $2(c)$  $2(c)$ ). As shown in Fig.  $6$ ,  $\delta'$  dropped abruptly as the fracture initiated at the critical value  $\delta_{c}$ , and then exhibited damping oscillation after fracture. If there was a noticeable amount of nonelastic deformation in the specimen, the centerline of the oscillation should be larger than the initial static displacement  $\delta_0$  (=0.05 mm). However,  $\delta'$  oscillated around  $\delta_{\rm n}$ , which was smaller than  $\delta_{\rm o}$ , suggesting that no great residual displacement was caused by viscoelastic or plastic deformation. This result was typical of impact tensile fracture behavior among specimens. Hence, we could disregard nonelastic energy  $E_n$  in Eqs. (2) and (3). We also



Fig. 9 External work  $U_{\text{ex}}$  as a function of fracture load  $P_{\text{c}}$ 

attributed the damping oscillation in Fig. [6](#page-3-0) to energy loss caused by elastic wave propagation in the specimen's loading axes.

The energy ratio  $E_e/U_{ex}$  in Eq. (3) was calculated as follows. First, amplitudes of the initial two oscillations were measured to estimate their attenuation (see Fig. [6](#page-3-0)). This attenuation was used to determine the intersection with falling curve  $\delta'$ , i.e., dynamic value  $\delta_{e}'$  just after fracture. Finally,  $\delta_e$  was determined using the following relationship (see Fig. [3](#page-2-0)):

$$
\delta_{\rm e} = \frac{\delta_{\rm e}'(P_o + P_{\rm c}')}{P_{\rm c}'}.\tag{4}
$$

Figures 10 and [11](#page-5-0) plot  $E_e/U_{ex}$  as a function of  $P_c$ . The  $E_e/U_{ex}$  of sample-1 decreased from 61% to 50% when  $P_c$ increased, while that of sample-2 increased slightly from 38% to 45%. The cause for this is not clear, but might be related to the dynamic behavior of crack propagation in the two samples.

#### Fracture energy  $E_f$

Figures 10 and [11](#page-5-0) also show the energy ratio  $E_f/U_{ex}$ derived from Eq. (2) by assuming  $E_n = 0$ . The  $E_f/U_{ex}$  for sample-1 increased with  $P_c$ , while that for sample-2 decreased. Sample-1 yielded about 39% in the region of small  $P_c$  and about 50% in the region of large  $P_c$ , and corresponding values for sample-2 were about 62% and 55%. This suggests that the fracture load and size of large particles can change fracture energy.

Energy release rate  $G_f$ 

Energy release rate  $G_f$  was estimated using the following equation:

$$
G_{\rm f} = E_{\rm f}/A_{\rm s}, \tag{5}
$$



Fig. 10 Energy ratios  $E_e/U_{ex}$  and  $E_f/U_{ex}$  as a function of fracture load  $P_c$  (Sample-1)

<span id="page-5-0"></span>

Fig. 11 Energy ratios  $E_e/U_{ex}$  and  $E_f/U_{ex}$  as a function of fracture load  $P_c$  (Sample-2)

where  $A_s$  is half the area of the total fracture surface. Figure 12 shows  $G_f$  values as a function of  $P_c$ .  $G_f$  for both samples increased with  $P_c$ , and sample-2 yielded much greater  $G_f$  values than sample-1 for a given  $P_c$ . This indicates that the rate of energy release increases with fracture load and is influenced by a sample's microstructures.

To determine why  $G_f$  increased with  $P_c$  and changed with particle size, we evaluated the mean crack velocity  $v_m$ in each specimen. This was achieved by measuring fall time  $\Delta t$  from  $P_c'$  to  $P = 0$  in the P'–t diagrams. Samples-1 and -2 in Fig. [4](#page-3-0) had  $\Delta t$  values of about 38  $\mu$ s and 89  $\mu$ s, respectively, and the corresponding  $v<sub>m</sub>$  values were about 190 m/s and 81 m/s.

Figure 13 plots mean crack velocity  $v_m$  as a function of fracture load  $P_c$ . Several interesting findings appeared in their relationships. First,  $v_m$  increased with  $P_c$ , similar to findings for energy release rate  $G_f$  (see Fig. 12). Second,  $v<sub>m</sub>$  values for the two samples were quite different: sample-1 yielded  $v_m$  values greater than 150 m/s, while values for sample-2 were less than 100 m/s. Finally, an opposite relationship appeared between  $G_f$  and  $v_m$ : sample-1 yielded high  $v_m$  and low  $G_f$  values, while sample-2 yielded low  $v_m$  and high  $G_f$  values. The cause of this is



Fig. 12 Energy release rate  $G_f$  as a function of fracture load  $P_c$ 



Fig. 13 Mean crack velocity  $v_m$  as a function of fracture load  $P_c$ 

not clear, but might be related to crack extension resistance from large particles since the two samples had the same total rubber content. The corresponding fracture surfaces of specimens tended to become rougher as  $G_f$ and  $v_m$  increased, implying that the energy consumed creating a fracture surface increases as the crack propagates at higher values of  $G_f$  and  $v_m$ .

#### **Conclusions**

We used an impact tensile device and an optical high-speed extensometer to examine brittle fractures of MBS resin with a bimodal rubber particle size distribution, and measured the impact load and displacement of single-edgecracked specimens to determine the external work  $U_{\text{ex}}$ applied to the specimen. We estimated the elastic energy  $E_e$ and nonelastic energy  $E_n$  just after fracture based on the oscillation of the split specimen. Fracture energy  $E_f$  was then determined and correlated with fracture load  $P_c$ . The energy release rate was evaluated with fracture surface  $A_s$ using  $G_f = E_f/A_s$ , and the mean crack velocity  $v_m$  was also estimated from the load-time diagram. In this experiment, total rubber content (28 wt%) and the size of small particles (about 140 nm) were unchanged, and the size of large particles were either about 490 nm or 670 nm. The following results were obtained.

- (1) Nonelastic energy  $E_n$  can be disregarded under the impact tensile loading conditions tested.
- (2) Fracture load  $P_c$ , displacement  $\delta_c$ , and external work  $U_{\text{ex}}$  increased when the size of large particles increased from about 490 nm to 670 nm for a given initial crack length.
- (3) Energy release rate  $G_f$  and mean crack velocity  $v_m$ increased with  $P_c$ .
- (4) The sample with the largest particle size (about 670 nm) yielded higher  $G_f$  values but lower  $v_m$  values for the same total rubber content.

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